

# Introduction to MATLAB

## 2. Vectors and matrices

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# Definition of vectors and matrices

A vector  $u = (u_1, u_2, \dots, u_n)$  is introduced in MATLAB as follows:

`>> u=[ u1, u2 , ..., un ]`    or    `>> u=[ u1 u2 ... un]`

Matrices are defined in a similar manner using `';` or `<Enter>` to change a line.

```
>> u=[ 1 2 3]
u =
     1     2     3
>> v=[1,-2,4,5,-2]
v =
     1    -2     4     5    -2
>>
>> A=[1 -2; 3 4]
A =
     1    -2
     3     4
>> A=[1 3 -4 2
0,1,0,1]
A =
     1     3    -4     2
     0     1     0     1
>>
```

# Matrix operations

Symbol	Operation
+	Addition
-	Subtraction
*	Multiplication
\	Left division
/	Right division
^	Power

■ the transpose  $A^T$  of a real matrix  $A$ , is denoted by  $A'$

■ Expressions

$$A * A * A \text{ and } A^3$$

where  $A$  is a square matrix are equivalent.

■ Scalar multiplication

$$x * A \text{ and } x * u$$

■ “Scalar division”:

$$A / x \text{ and } u / x$$

■ “Scalar addition”:

$$A - x \text{ and } u + x$$

# Left and right division

**A\b**

Solution of  $Ax = b$

**b/A**

Solution of  $xA = b$

# Elementary matrices

function	
eye zeros ones rand randn pascal magic hilb invhilb	

1) **eye(m,n)** and **eye([m n])** are equivalent.

2) **ones(n)** and **ones(n,n)** are equivalent.

**See:    help elmat**

# Defining vectors with a step

$$u = [u_1 : step : u_{last}]$$

$$u = u_1 : step : u_{last}$$

$$u = [u_1 : u_{last}]$$

$$u = u_1 : u_{last}$$

**Last  
possible  
value**

**step=1**

Όπως φαίνεται στο παράδειγμα που ακολουθεί η ίδια ιδέα μπορεί να χρησιμοποιηθεί για την κατασκευή πινάκων.

### Παράδειγμα 2.3.2

Θα κατασκευάσουμε τους πίνακες

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 10 & 8 & 6 & 4 & 2 \end{bmatrix} \quad \text{και} \quad B = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 2 & 4 & 6 & 8 & 10 \\ 3 & 6 & 9 & 12 & 15 \end{bmatrix}.$$

```
>> A=[1:5;10:-2:2]
```

```
A =
```

```
     1     2     3     4     5
    10     8     6     4     2
```

```
>> B=[1:5;2:2:10;3:3:15]
```

```
B =
```

```
     1     2     3     4     5
     2     4     6     8    10
     3     6     9    12    15
```

# Defining subvectors and submatrices

- $A(i,j) \rightarrow a_{ij}$
- to  $A(:,j) \rightarrow j$  column of  $A$
- $A(i, :) \rightarrow i$  line of  $A$
- $A(m:n,p:s) \rightarrow$  submatrix
- to  $A(\text{end},:) \rightarrow$  last line of  $A$
- to  $A(:, \text{end}) \rightarrow$  last column of  $A$



Diagram illustrating matrix indexing for a 4x5 matrix  $A$ :

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \end{bmatrix}$$

Annotations:

- $A(:,2)$  points to the second column (elements  $a_{12}, a_{22}, a_{32}, a_{42}$ ).
- $A(2,3)$  points to the element  $a_{23}$ .

Diagram illustrating matrix indexing for a 4x5 matrix  $A$  with highlighted submatrices:

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \end{bmatrix}$$

Annotations:

- $A(1:3,1)$  points to the first column of rows 1 to 3 (elements  $a_{11}, a_{21}, a_{31}$ ).
- $A(1:3,3:5)$  points to the submatrix of rows 1 to 3 and columns 3 to 5 (elements  $a_{13}, a_{14}, a_{15}, a_{23}, a_{24}, a_{25}, a_{33}, a_{34}, a_{35}$ ).
- $A(4,:)$  points to the fourth row (elements  $a_{41}, a_{42}, a_{43}, a_{44}, a_{45}$ ).

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \\ 13 & 14 & 15 & 16 \end{bmatrix}$$

είναι ο εξής:

```
>> u=1:16
```

```
u =
Columns 1 through 13
    1     2     3     4     5     6     7     8     9    10
11    12    13
Columns 14 through 16
    14    15    16
```

```
>> A=zeros(4);
```

```
>> A(:)=u
```

```
A =
    1     5     9    13
    2     6    10    14
    3     7    11    15
    4     8    12    16
```

```
>> A=A'
```

```
A =
    1     2     3     4
    5     6     7     8
    9    10    11    12
   13    14    15    16
```

# Element by element operations

Function of a vector or a matrix!

$\sin(u)$

or

$\exp(A)$

Element by element operations:

$u.^2$

$1./u$

$A.^3$

$u.*v$

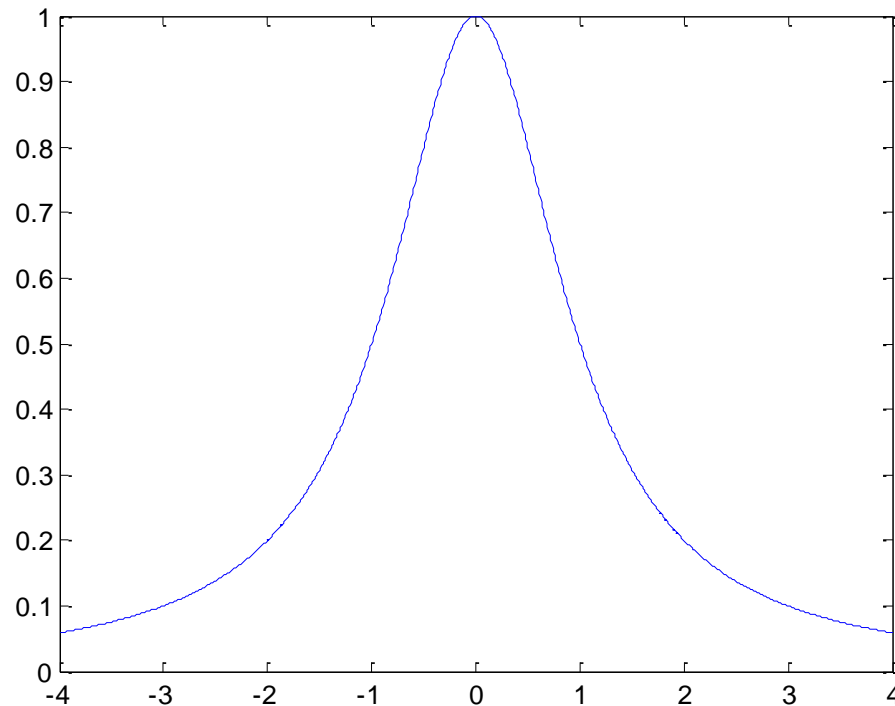
$A.*B$

$C=2.^A$

# Example

$$f(x) = \frac{1}{x^2 + 1}$$

```
>> x=-4:0.01:4;  
>> y=1./ ( x.^2+1) ;  
>> plot(x,y)
```



See also: **linspace**

# Functions for vectors

Συνάρτηση	Ερμηνεία
<b>max</b>	μέγιστο στοιχείο διανύσματος
<b>min</b>	ελάχιστο στοιχείο διανύσματος
<b>length</b>	μήκος διανύσματος
<b>sort</b>	ταξινόμηση σε αύξουσα σειρά
<b>sum</b>	άθροισμα στοιχείων
<b>prod</b>	γινόμενο στοιχείων
<b>norm</b>	νόρμα διανύσματος
<b>median</b>	διάμεσος
<b>mean</b>	μέση τιμή
<b>std</b>	τυπική απόκλιση

# Functions for matrices

Function	
<b>max</b> <b>min</b> <b>diag</b> <b>triu</b> <b>tril</b> <b>size</b> <b>length</b> <b>norm</b> <b>det</b> <b>trace</b> <b>rank</b> <b>inv</b> <b>rref</b> <b>eig</b> <b>poly</b> <b>cond</b>	

# MATRIX CONCATENATION

```
>> A=rand(2) ; B=rand(2) ; C=rand(2) ; D=rand(2) ;
```

```
>> [A B C]
```

```
ans =
```

0.8147	0.1270	0.6324	0.2785	0.9575	0.1576
0.9058	0.9134	0.0975	0.5469	0.9649	0.9706

```
>> [A; B; C]
```

```
ans =
```

0.8147	0.1270
0.9058	0.9134
0.6324	0.2785
0.0975	0.5469
0.9575	0.1576
0.9649	0.9706

```
>> [A B; C D]
```

```
ans =
```

0.8147	0.1270	0.6324	0.2785
0.9058	0.9134	0.0975	0.5469
0.9575	0.1576	0.9572	0.8003
0.9649	0.9706	0.4854	0.1419

See also: **repmat** and **cat**

# Assigning values to submatrices

**$A(1:3,1:4)=0$**

**$A(3,:)=\exp(1)$**

**$A(:,3:4)=\pi$**

**$A(:,\text{end})=1$**



# Comment

$A'$  Conjugate transpose of  $A$

$A.'$  Transpose of  $A$

$A.'''$  Conjugate of  $A$

# Example

```
>> A=[ 1+i 2-3i  
4+2i i]
```

```
A =
```

```
1.0000 + 1.0000i    2.0000 - 3.0000i  
4.0000 + 2.0000i    0.0000 + 1.0000i
```

```
>> A'
```

```
ans =
```

```
1.0000 - 1.0000i    4.0000 - 2.0000i  
2.0000 + 3.0000i    0.0000 - 1.0000i
```

```
>> A.'
```

```
ans =
```

```
1.0000 + 1.0000i    4.0000 + 2.0000i  
2.0000 - 3.0000i    0.0000 + 1.0000i
```

```
>> A.''
```

```
ans =
```

```
1.0000 - 1.0000i    2.0000 + 3.0000i  
4.0000 - 2.0000i    0.0000 - 1.0000i
```

```
>>
```

# Comment

**MATLAB increases the dimensions of a matrix when necessary.**

```
>> A=ones(3)
```

```
A =
```

```
 1  1  1
 1  1  1
 1  1  1
```

```
>> A(5,6)=3
```

```
A =
```

```
 1  1  1  0  0  0
 1  1  1  0  0  0
 1  1  1  0  0  0
 0  0  0  0  0  0
 0  0  0  0  0  3
```

# Other possibilities

$A(:, k) = []$

Delete column k

$A(k, :) = []$

Delete line k

$A(k:m, :) = []$

Delete lines k to m

$A(:, k:m) = []$

Delete columns k to m

# Example

```
>> A=eye(6); A(:,3:4)=[
```

```
A =
```

1	0	0	0
0	1	0	0
0	0	0	0
0	0	0	0
0	0	1	0
0	0	0	1

```
>> A=[eye(2) zeros(2); zeros(2,4); zeros(2) eye(2)]
```

```
A =
```

1	0	0	0
0	1	0	0
0	0	0	0
0	0	0	0
0	0	1	0
0	0	0	1

```
>> A=zeros(6,4); A(1:2,1:2)=eye(2); A(5:6,3:4)=eye(2)
```

```
A =
```

1	0	0	0
0	1	0	0
0	0	0	0
0	0	0	0
0	0	1	0
0	0	0	1

```
>>
```



***Thank you!!***